

Problem 1. *Let f be a function and a a point.*

(a) *Define “derivative of f at a ” using only words.*

(b) *Define “derivative of f at a ” using only symbols.*

(c) *Illustrate “derivative of f at a ” using a picture (and explain the picture).*

(d) *What is the notation for the derivative of f at a ?*

Problem 2. *Compute the derivative of $f(x) = \pi x + e$ at $a = 7$.*

Problem 3. *Suppose f is a linear function with slope m , and a is some number. What is the derivative of f at a ? (Don't just use your intuition. Show me the calculation.)*

Problem 4. *Suppose you're 10 miles north of Urbana, driving at 65 miles/hour. How many miles north of Urbana do you expect to be after 10 seconds pass?*

Problem 5. *Suppose you know that the derivative of $\sin(x)$ at $a = \pi/3$ is $1/2$ (which is, in fact, true). Use this to estimate $\sin(1)$.*

Problem 6. *If a rock is thrown upward on Mars with a velocity of 10 m/s, its height (in meters) after t seconds is given by $H(t) = 10t - 1.86t^2$.*

(a) *Does the formula make sense (what is the position and velocity of the rock at time $t = 0$?*

(b) *Find the velocity of the rock after one second.*

(c) *Find the velocity of the rock at time $t = a$.*

(d) *When will the rock hit the surface? With what velocity?*