

Warning: one of the tasks below is impossible.

**Problem 1.** (a) *If someone says “the function  $f$  is differentiable”, what does that actually mean? Be as precise as you can.*

(b) *Draw a function that is continuous but not differentiable.*

(c) *Draw a function that is differentiable but not continuous.*

(d) *Draw a negative function  $f$  so that  $f'$  is positive but  $f''$  is negative.*

**Problem 2.** *Compute the following derivatives.*

(a)  $f'(x)$  for  $f(x) = \pi x + e$ .

(b)  $f''(x)$  for  $f(x) = ax + b$ .

(c)  $f^{(2013)}$  for  $f(x) = ax + b$ .

(d)  $f'(0)$  for  $f(x) = x^2 \sin(1/x)$ .

**Problem 3.** *(Extra; won't be on a test or quiz, but still good practice.)*

(a) *Is it true that the derivative of an odd function is always even?*

(b) *Is every function that is defined for all real numbers differentiable at least somewhere?*