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**Problem 2.** *Decode the message written in Caesar cipher (warning: it's in Latin).*  
*HW WX EUXWH*

**Problem 3.** *The following was encoded using a shift cipher. Guess the shift and decode the message.*  
*B TIJGU DJQIFS*

**Problem 4.** *Use a 2-letter shift cipher to encode "hello world".*

**Problem 5.** *Read the following:*

Another old encryption scheme consists of writing backwards. For example, some of Leonardo da Vinci's notes are written backwards so others would have trouble reading them. And then there's the "boustrophedon" sometimes used in Ancient Greece — and in this paragraph.

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**Problem 6.** *Completely factor the following numbers into primes:*

(a) 24

(b) 385

(c) 223

**Problem 7.** *Use the Sieve of Aristophanes to find all the primes between 90 and 100.*

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**Problem 8.** *Suppose you are sending the number 791931.*

(a) *Compute the basic checksum.*

(b) *Compute the 1 – 3 – 1 – 3 checksum.*

**Problem 9.** *Most credit cards implement the Luhn Algorithm (patented in 1960), which works as follows (let's use the example 4485723586944236):*

1. *Remove the last digit, which is the checksum (6, leaving 448572358694423).*
2. *Double every other remaining digit (8,4,16,5,14,2,6,5,16,6,18,4,8,2,6).*
3. *Add up all the digits ( $8 + 4 + 1 + 6 + 5 + 1 + 4 + 2 + 6 + 5 + 1 + 6 + 6 + 1 + 8 + 4 + 8 + 2 + 6 = 84$ ).*
4. *Take the last digit of your sum (4) and subtract it from 10 (6). That is the checksum from 1.*

*Are the following valid credit card numbers?*

(a) *4929085163644314*

(b) *5143982419828804*