

Problem 1. (1 point) Is the function $f(x) = 2x + 1$ one-to-one? Justify your answer.

Problem 2. (1 point) What is $\sin^{-1}(\sqrt{2}/2)$?

Problem 3. (2 points) Here are seven of the Limit Laws:

- 1) $\lim_{x \rightarrow a} [f(x) + g(x)] = \lim_{x \rightarrow a} f(x) + \lim_{x \rightarrow a} g(x)$
- 2) $\lim_{x \rightarrow a} [f(x) - g(x)] = \lim_{x \rightarrow a} f(x) - \lim_{x \rightarrow a} g(x)$
- 3) $\lim_{x \rightarrow a} [cf(x)] = c \lim_{x \rightarrow a} f(x)$
- 4) $\lim_{x \rightarrow a} [f(x)g(x)] = (\lim_{x \rightarrow a} f(x)) \cdot (\lim_{x \rightarrow a} g(x))$
- 5) $\lim_{x \rightarrow a} [f(x)/g(x)] = (\lim_{x \rightarrow a} f(x)) / (\lim_{x \rightarrow a} g(x))$ if $\lim_{x \rightarrow a} g(x) \neq 0$
- 6) $\lim_{x \rightarrow a} c = c$
- 7) $\lim_{x \rightarrow a} x = a$

Using **only** these rules, compute the following limit. Use only one rule in each step of your calculation, and tell me which rule you are using.

$$\lim_{x \rightarrow 1} \frac{x + 1}{3} =$$

Problem 4. (2 points each) Compute the following limits, or explain why they don't exist. Make sure to show your work.

(a) $\lim_{h \rightarrow 0} \frac{(3+h)^2 - 9}{h}$

(b) $\lim_{x \rightarrow 1} f(x)$, where $f(x) = \begin{cases} x^3 & \text{if } x < 1 \\ \sqrt[13]{x} & \text{if } x > 1 \end{cases}$

(c) $\lim_{x \rightarrow 0} x \sin(\pi/x)$