Problem 1. A farmer wants to fence an area of 1.5 million square feet in a rectangular field and then divide it in half with a fence parallel to one of the sides of the rectangle. How can he do this so as to minimize the cost of the fence?

Problem 2. A box with a square base and an open top must have a volume of 32,000 cm³. Find the dimensions of the box that minimize the amount of material used.

Problem 3. A manufacturer has been selling 1000 TVs a week at \$450 each. A market survey indicates that for each \$10 discount offered to the buyer, the number of TVs sold will increase by 100 per week.

- (a) Find the demand function. That is, how many TVs are sold at each discount level?
- (b) How large a discount should the company offer to maximize the revenue?

(c) Suppose that each week it costs \$86,000 to run the business, and each TV costs \$150 to make and get to the customer. What discount would maximize the company's profits?