

Two pages, 4 problems, 10 points. Explain each answer, but don't simplify it.

Problem 1 (2 points). Write $1/5$ as a percent value (%) and as parts per million (ppm).

20%

200,000ppm

Problem 2 (1 point each). You have 10 balls in a bag: 3 blue and striped, 2 blue and solid, 4 green and striped, 1 green and solid.

(a) What are the chances of randomly picking a ball that is neither blue nor striped?

The green and solid ball is the only one that is not blue or striped. So $1/10$.

(b) Suppose you randomly pick a blue ball. What are the chances it is striped?

5 blue balls, 3 of them striped.
So $3/5$.

Problem 3 (2 points). You are about to buy something for \$130. You have a 15% off coupon and a \$20 coupon. Which one should you use?

$$15\% \cdot 130 = 13 + 6.50 = 19.50.$$

\uparrow \uparrow
 10% 5%

So the \$20 coupon is a better value.

Problem 4 (2 points each). In a city of 100,000 people, there are 300 werewolves. You have developed a werewolf test that successfully identifies a werewolf 98% of the time. It also has a false-positive rate of 1%. You test the entire population for being werewolves.

(a) How many non-werewolves did you (probably) diagnose as being werewolves?

There are $100,000 - 300 = 99,700$ non-werewolves.

1% of them get diagnosed as werewolves.

So 997.

(b) How many werewolves did you (probably) diagnose as being werewolves?

$$300 \times 98\% = 3 \times 98 = ~~294~~ \quad \boxed{294}$$

median & mean

